

5. UNSYMMETRICAL BENDING

Symmetrical bending:

The plane of loading (or) plane of bending is coincide. lie in a plane that contains centroidal axis of cross-section the bending is called "symmetric bending."

Unsymmetrical bending:

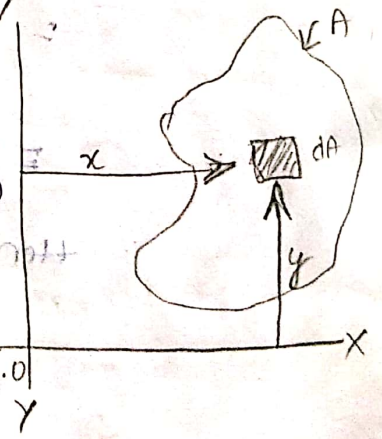
The plane of loading or bending does not lie in a plane that contains ^{principle} centroidal axis of cross-section the bending is called "unsymmetrical bending"

principle axis:

If the two axis about which product of inertia becomes zero, the true axis are called "principle axis". The moment of inertia about principle axis is called "principle moment of inertia".

Product of inertia:

Consider a plane area 'A' in that elemental area dA which is at a distance of 'x' from y-y axis, 'y' from x-x axis respectively.



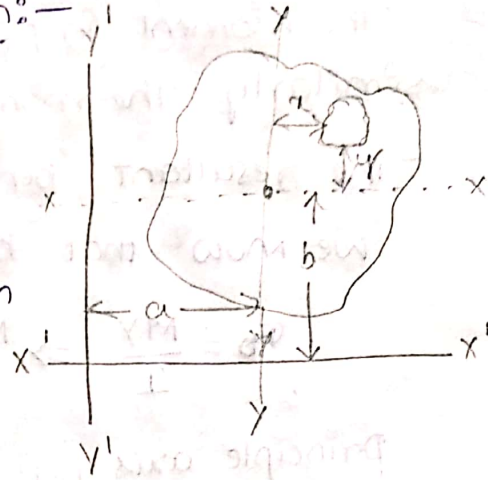
In that $\int xy \cdot dA$ is defined as product of inertia of cross-section. Then it can be Mathem-

atically written as

$$I_{xy} = \int xy \cdot dA = \int_0^A xy \cdot dA.$$

parallel axis theorem:-

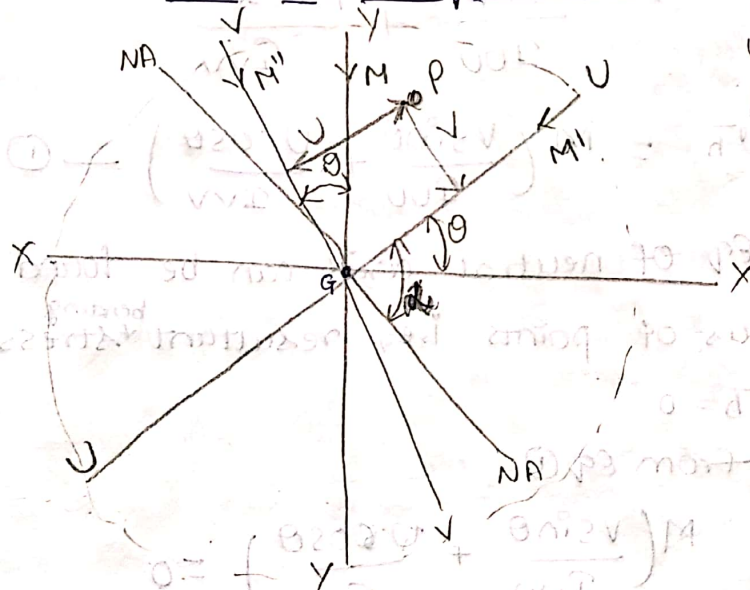
Let $x-x$ and $y-y$ are centroidal axis x' and y' are co-ordinate axis. It is possible to transform the moment of inertia about co-ordinate axis.



∴ According to this theorem

$$I_{x'y'} = I_{xy} + Aab.$$

Stresses due to unsymmetrical bending:-



UU & VV are principle axis.

'G' be the centroid of the section, $x-x$, $y-y$ are co-ordinate axis passing through the center of gravity 'G'. Let NA be the Neutral axis. UU and v-v are principle axis. an angle ' θ ' to $x-x$ and $y-y$ axis.

Let us determine stress distribution over the diagram.

The moment 'M' in the plane y-y can be resolved into components in the plane of U-U and V-V principle axes.

The moment in plane U-U = $M' = M \sin \theta$.
 Similarly the moment in plane V-V = $M'' = M \cos \theta$.

The resultant bending stress at point 'p' is
 We know that bending stress $\sigma_b = \frac{M}{Z} \left(z = \frac{I}{Y} \right)$

$$\sigma_b = \frac{MY}{I} \Rightarrow \frac{M(U+V)}{I} = \frac{M'U}{I_{UU}} + \frac{M''V}{I_{VV}}$$

principle axis U-U corresponding moment = M'

$$\sigma_b = \frac{M'V}{I_{UU}} + \frac{M''U}{I_{VV}}$$

$$= \frac{M \sin \theta \cdot V}{I_{UU}} + \frac{M \cos \theta \cdot U}{I_{VV}}$$

$$\sigma_b = M \left(\frac{V \sin \theta}{I_{UU}} + \frac{U \cos \theta}{I_{VV}} \right) \quad \text{--- (1)}$$

The Eq of neutral axis can be found by finding the locus of points i.e., resultant bending stress is 'zero'.

⊙ $\sigma_b = 0$

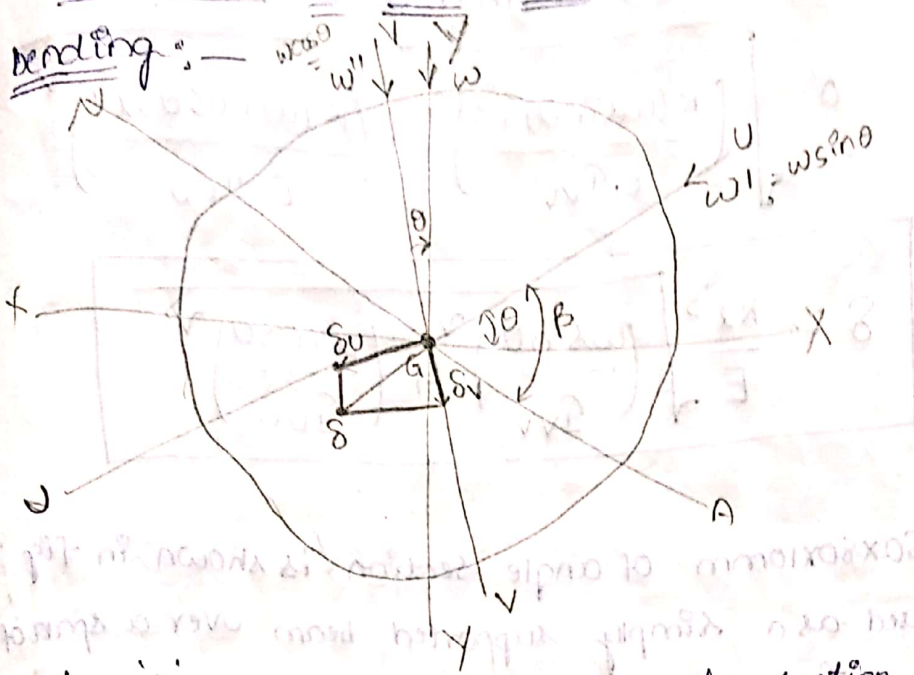
then from Eq (1)

$$M \left(\frac{V \sin \theta}{I_{UU}} + \frac{U \cos \theta}{I_{VV}} \right) = 0$$

$$\frac{V \sin \theta}{I_{UU}} + \frac{U \cos \theta}{I_{VV}} = 0$$

The max. stress will occur at a point which is the greatest distance from the neutral axis.

Deflection of beams due to unsymmetrical



Let 'G' be the centroid of the section. X-X and Y-Y are co-ordinate axis which is passing through the center. U-U and V-V are principle axis inclined at an angle ' θ ' with X-X and Y-Y axis.

Let 'w' be the load acting along line Y-Y on section of beam. The load 'w' can be resolved into two components along U-U $= w' = w \sin \theta$, similarly along V-V $= w'' = w \cos \theta$

Let ' δ_U ' be the deflection caused by the component of w' ($w \sin \theta$) along line 'GU' the bending occurs about V-V axis. Similarly ' δ_V ' deflection caused by the component of w'' ($w \cos \theta$) along line 'GV' the bending occurs about U-U axis.

The depending of the end conditions of the beam. The values of ' δ_U ' and ' δ_V ' are given by

$$\delta_U = \frac{k(w \sin \theta) l^3}{E I_{VV}}$$

$$\delta_V = \frac{k(w \cos \theta) l^3}{E I_{UU}}$$

'k' is constant depending upon end conditions of the beam and position of load.

'l' = length of the beam

E = Young's modulus ..

The resultant deflection $\delta = \sqrt{\delta_u^2 + \delta_v^2}$

$$\delta = \sqrt{\left(\frac{K(w \sin \theta) l^3}{E \cdot I_{VV}}\right)^2 + \left(\frac{K(w \cos \theta) l^3}{E \cdot I_{UU}}\right)^2}$$

$$\therefore \delta = \frac{K l^3}{E} \sqrt{\left(\frac{w \sin \theta}{I_{VV}}\right)^2 + \left(\frac{w \cos \theta}{I_{UU}}\right)^2}$$

29/12/2020

① A 80x80x10mm of angle section is shown in fig. It is used as a simply supported beam over a span of 2.4m. It carries a load of 400N along the line YG where G is the centroid of the section.

Calculate the (i) stress at points A, B, and C of the mid section of the beam. (ii) Deflection of the beam at the mid section, and its direction with the load line. (iii) position of Neutral axis.

Take $E = 200 \text{ GN/m}^2$

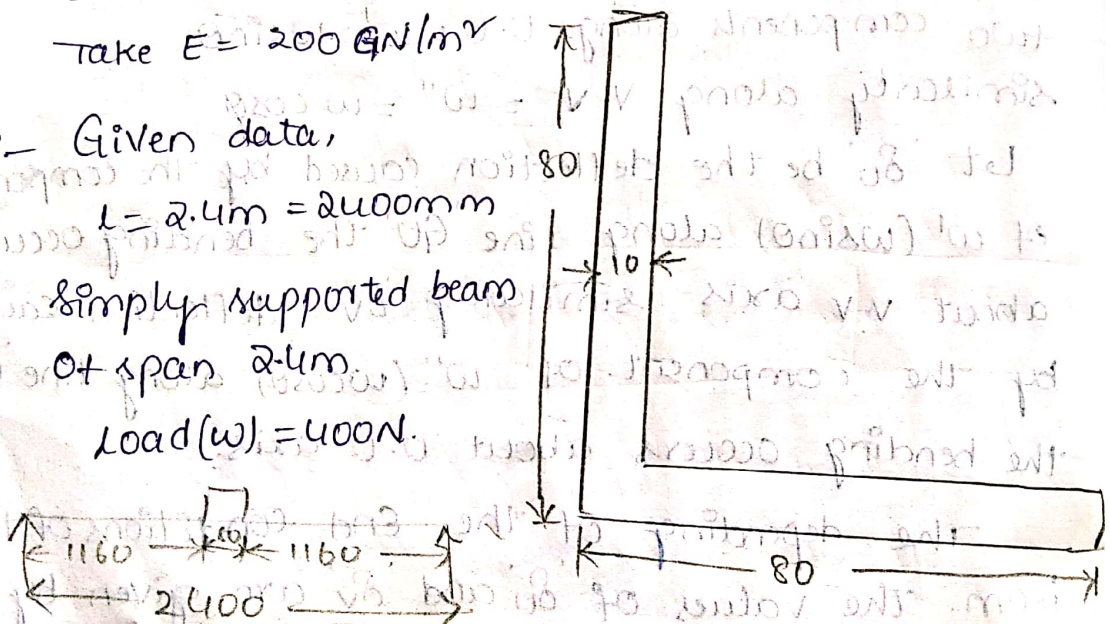
Sol.:- Given data,

$$l = 2.4 \text{ m} = 2400 \text{ mm}$$

Simply supported beam

of span 2.4m.

$$\text{Load } (w) = 400 \text{ N}$$



Simply supported beam point load at mid span

$$B.M = \frac{wl}{4} = \frac{400 \times 2400}{4} = 240 \text{ KN.m} = 2.4 \times 10^5 \text{ N.m}$$

$$\frac{x}{a} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2}$$

$$= \frac{(80 \times 10) \times \left(\frac{80}{2}\right) + (70 \times 10) \times \left(\frac{10}{2}\right)}{(80 \times 10) + (70 \times 10)}$$

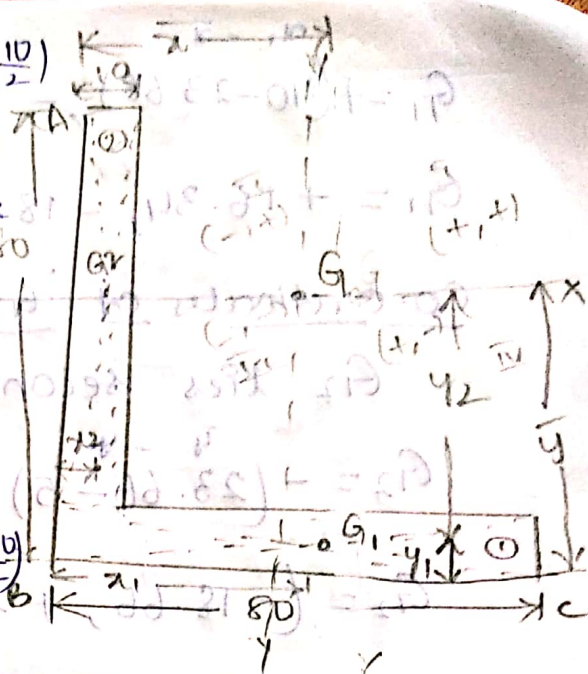
$x_1 =$ distance from G_1 to extreme End. 80

$$\therefore \bar{x} = 23.66 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$$

$$= \frac{(80 \times 10) \left(\frac{10}{2}\right) + (70 \times 10) \left(10 + \frac{70}{2}\right)}{(80 \times 10) + (70 \times 10)}$$

$$\therefore \bar{y} = 23.66 \text{ mm}$$



The given section is Equal angle section.

$$I_{xx} = \left[\frac{bd^3}{12} + A_1 (\bar{y} - y_1)^2 \right] + \left[\frac{bd^3}{12} + A_2 (\bar{y} - y_2)^2 \right]$$

$$= \left[\frac{80 \times 10^3}{12} + (80 \times 10) \left(23.66 - \frac{10}{2} \right)^2 \right] + \left[\frac{10 \times 70^3}{12} + (70 \times 10) \left(23.66 - 45 \right)^2 \right]$$

$$= 285223.14 + 604610.25$$

$$\therefore I_{xx} = 889833.39 \text{ mm}^4 = 8.89 \times 10^5 \text{ mm}^4$$

$$I_{yy} = \left[\frac{db^3}{12} + A_1 (\bar{x} - x_1)^2 \right] + \left[\frac{db^3}{12} + A_2 (\bar{x} - x_2)^2 \right]$$

$$= \left[\frac{10 \times 80^3}{12} + (80 \times 10) \left(23.66 - \frac{80}{2} \right)^2 \right] +$$

$$\left[\frac{70 \times 10^3}{12} + (70 \times 10) \left(23.66 - 5 \right)^2 \right]$$

$$= 640263.14 + 249570.2$$

$$\therefore I_{yy} = 8.89 \times 10^5 \text{ mm}^4$$

Fix the Quadrants of G_1 .

G_1 lies fourth Quadrant (+, -)

$$G_1 = + (40 - 23.66), - (23.66 - 5)$$

$$G_1 = + 16.34, - 18.66$$

Co-ordinates of G_2

G_2 lies second quadrant (-, +)

$$G_2 = - (23.66 - 5), + (45 - 23.66)$$

$$G_2 = (- 18.66, + 21.34)$$

* product of inertia (I_{xy}) = (Area of rectangle \times multiplication of co-ordinates) + (Area of rectangle \times multiplication of co-ordinates)

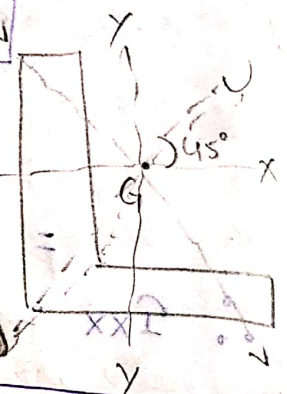
$$= (80 \times 10) 16.34 \times (- 18.66) + (- 70 \times 10) \times (- 18.66) \times 21.34$$

$$I_{xy} = - 5.22 \times 10^5 \text{ mm}^4$$

principle moment of inertia :-

Let U-U and V-V are principle axis.

\therefore principle moment of inertia I_{UU}



$$I_{UU} = \frac{1}{2} [I_{xx} + I_{yy}] + \frac{1}{2} [I_{xx} - I_{yy}] \cos 2\theta - I_{xy} \sin 2\theta$$

$$= \frac{1}{2} [8.89 \times 10^5 + 8.89 \times 10^5] + \frac{1}{2} [8.89 \times 10^5 - 8.89 \times 10^5] \cos 2 \times 45^\circ - (- 5.22 \times 10^5) \times \sin 2 \times 45^\circ$$

$$\therefore I_{UU} = 1411000 = 14.11 \times 10^5 \text{ mm}^4$$

w.k.that M.I of principle axis = M.I of co-ordinate axis.

$$I_{UU} + I_{VV} = I_{xx} + I_{yy}$$

$$I_{VV} = I_{xx} + I_{yy} - I_{UU}$$

$$= (8.89 \times 10^5) + (8.89 \times 10^5) - (14.12 \times 10^5)$$

$$\therefore I_{VV} = 3.66 \times 10^5 \text{ mm}^4$$

(i) calculation of stresses at point 'A'

$$B.M = M = 2.4 \times 10^5 \text{ N}\cdot\text{mm}$$

$$M' = M \sin \theta = 2.4 \times 10^5 \times \sin 45^\circ = 1.69 \times 10^5 \text{ N}\cdot\text{mm}$$

$$M'' = M \cos \theta = 2.4 \times 10^5 \times \cos 45^\circ = 1.69 \times 10^5 \text{ N}\cdot\text{mm}$$

Stresses co-ordinates at 'A'

$$A = (-23.66, +56.34)$$

$$U = x \cos \theta + y \sin \theta$$

$$= -23.66 \cos 45^\circ + 56.34 \sin 45^\circ$$

$$\therefore U = 23.10 \text{ mm}$$

$$V = \frac{du}{d\theta} = -x \sin \theta + y \cos \theta$$

$$= (-23.66) \sin 45^\circ + 56.34 \cos 45^\circ$$

$$\therefore V = 56.56 \text{ mm}$$

$$\sigma_A = \frac{M'U}{I_{VV}} + \frac{M''V}{I_{UU}} = 50$$

$$= \left(\frac{1.69 \times 10^5 \times 23.1}{3.66 \times 10^5} \right) + \left(\frac{1.69 \times 10^5 \times 56.56}{14.11 \times 10^5} \right)$$

$$= 17.43 \text{ N/mm}^2$$

$$B = (-23.66), (-23.66)$$

$$U = x \cos \theta + y \sin \theta$$

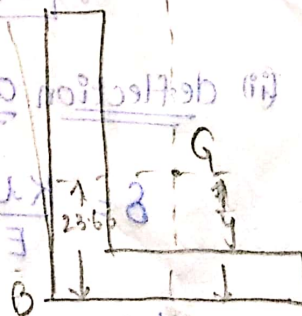
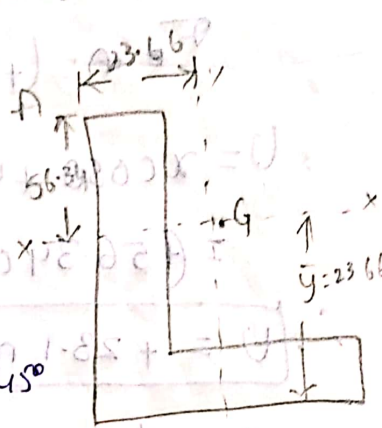
$$= (-23.66 \cos 45^\circ) + (-23.66 \sin 45^\circ)$$

$$U = -33.46 \text{ mm}$$

$$V = \frac{du}{d\theta} = -x \sin \theta + y \cos \theta$$

$$= -(-23.66 \sin 45^\circ) + (-23.66 \cos 45^\circ)$$

$$V = 0$$



$$\sigma_B = \frac{M'U}{I_{VV}} + \frac{M''V}{I_{UU}}$$

$$= \frac{1.69 \times 10^5 \times (-33.46)}{3.66 \times 10^5} + \frac{1.69 \times 10^5 \times 0}{14.11 \times 10^5}$$

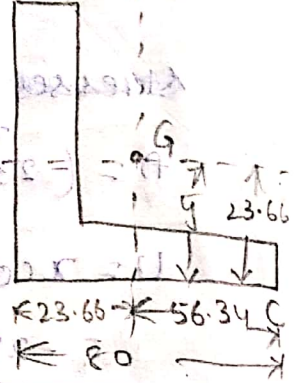
$$\sigma_B = 15.45 \text{ N/mm}^2$$

$$E \cdot A = (+56.34), \quad (23.66)$$

$$U = x \cos \theta + y \sin \theta$$

$$= (+56.34 \cos 45^\circ) + (23.66 \sin 45^\circ)$$

$$\therefore U = +23.1 \text{ mm}$$



$$V = \frac{du}{d\theta} = -x \sin \theta + y \cos \theta$$

$$= -56.34 \sin 45^\circ + (23.66 \cos 45^\circ)$$

$$\therefore V = -56.56 \text{ mm}$$

$$\sigma_C = \frac{M'U}{I_{VV}} + \frac{M''V}{I_{UU}}$$

$$= \frac{1.69 \times 10^5 \times 23.1}{3.66 \times 10^5} + \frac{1.69 \times 10^5 \times (-56.56)}{14.11 \times 10^5}$$

$$= 10.66 + (-6.74)$$

$$\therefore \sigma_C = 3.88 \text{ N/mm}^2$$

(ii) deflection of the beam :-

$$\delta = \frac{K \lambda^3 w}{E} \sqrt{\left(\frac{\sin \theta}{I_{VV}}\right)^2 + \left(\frac{\cos \theta}{I_{UU}}\right)^2}$$

The end condition is simply supported $K = \frac{1}{48}$

$$w = 400 \text{ N}, \quad l = 2400 \text{ mm}, \quad E = 200 \text{ GN/m}^2$$

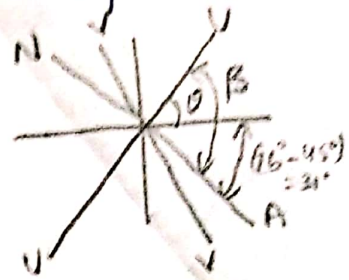
$$I_{UU} = 14.12 \times 10^5 \text{ mm}^4, \quad I_{VV} = 3.66 \times 10^5 \text{ mm}^4, \quad E = 200 \times 10^9 \text{ N/m}^2$$

$$\theta = 45^\circ, \quad E = 200 \times 10^3 \text{ N/mm}^2$$

$$\begin{aligned}
 \delta &= \frac{1}{48} \times \frac{2400^3}{200 \times 10^3} \times 400 \sqrt{\left(\frac{6 \sin 45^\circ}{366 \times 10^5}\right)^2 + \left(\frac{\cos 45^\circ}{14.12 \times 10^5}\right)^2} \\
 &= 576000 \sqrt{3.98 \times 10^{-12}} \\
 \therefore \delta &= \boxed{1.14 \text{ mm}}
 \end{aligned}$$

(ii) Let θ = Angle b/w co-ordinate axis to principle axis, β = Angle b/w Neutral axis to principle axis

$$\begin{aligned}
 -\tan \beta &= \frac{I_{UV}}{I_{VV}} \cdot \tan \theta \\
 &= \frac{14.12 \times 10^5}{3468 \times 10^5} \times \tan 45^\circ
 \end{aligned}$$



$$-\tan \beta = 4.80857 \Rightarrow \beta = \tan^{-1}(3.857)$$

$$\therefore \beta = 76^\circ 28'$$

Position of Neutral axis

The Neutral axis is perpendicular to line of deflection angle. (90° - deflection angle)

$$= 90^\circ - 31^\circ = 59^\circ$$

① A cantilever of I-section is subjected to a load of 200N at the free end. Determine the resulting stress at corners A & B on the fixed section of cantilever.

→ let $X'-x'$ and $Y'-y'$ are co-ordinate axis.

* $X-X$ and $Y-Y$ (or) $U-U$ and $V-V$ are principle axis.

Let us assume I-section is a symmetrical section then moment of inertia of principle axis

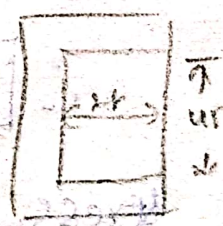
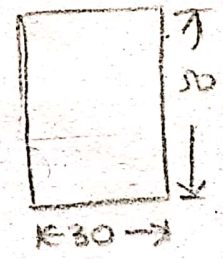
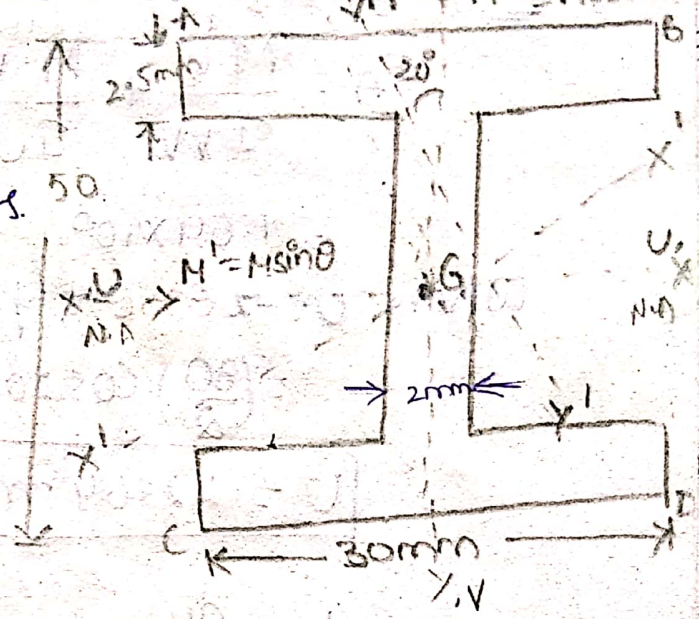
$$I_{xx} = I_{uu} = \frac{B D^3}{12} - \frac{b d^3}{12}$$

$$= \frac{30 \times 50^3}{12} - \frac{28 \times 45^3}{12}$$

$$= 99875 \text{ mm}^4$$

$$I_{yy} = I_{vv} = 2 \left(\frac{2.5 \times 30^3}{12} \right) + \frac{45 \times 2^3}{12}$$

$$= 11280 \text{ mm}^4$$



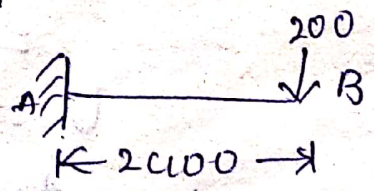
Given support beam is cantilever the I-section acts at free end.

Cantilever beam with point load at free end.

$$B.M = w l$$

$$= 200 \times 2400$$

$$= 480000 \text{ N.mm}$$



$$M^I = M \sin \theta = 480000 \times \sin 20^\circ = 1.64 \times 10^5 \text{ N}$$

$$M^{II} = M \cos \theta = 480000 \times \cos 20^\circ = 4.51 \times 10^5 \text{ N}$$

Stress at a θ \rightarrow 4th Quadrant

$$\sigma_A = \frac{M^I U}{I_{VV}} + \frac{M^{II} V}{I_{UU}} \quad (-, +)$$

where $U = x \cos \theta + y \sin \theta$

$$= \left(\frac{30}{2}\right) \cos 20^\circ + \left(\frac{50}{2}\right) \sin 20^\circ$$

$$\therefore \boxed{U = 22.64 \text{ mm}} - 5.54 \text{ mm}$$

$$V = \frac{du}{d\theta} = -(x \sin \theta) + y \cos \theta$$

$$= -\left(\frac{30}{2} \sin 20^\circ\right) + \left(\frac{50}{2}\right) \cos 20^\circ$$

$$= 18.362 \text{ mm}$$

$$\sigma_A = \frac{1.64 \times 10^5 \times 22.64}{11280} + \frac{4.51 \times 10^5 \times 18.362}{99875}$$

$$\therefore \boxed{\sigma_A = 49.208 \text{ N/mm}^2}$$

Stress at a θ \rightarrow at 1st Quadrant

$$\sigma_B = \frac{M^I U}{I_{VV}} + \frac{M^{II} V}{I_{UU}} \quad (+, +)$$

where, $U = x \cos \theta + y \sin \theta$

$$= 15 \cos 20^\circ + 25 \sin 20^\circ$$

$$U = 22.64 \text{ mm}$$

$$V = \frac{du}{d\theta} = -x \sin \theta + y \cos \theta$$

$$= -\left(\frac{30}{2} \sin 20^\circ\right) + 25 \cos 20^\circ$$

$$V_{CB} = 18.36 \text{ mm}$$

$$\sigma_B = \frac{1.64 \times 10^5 \times 22.64}{11280} + \frac{18.36 \times 4.51 \times 10^5}{99875}$$

$$\sigma_B = 412.07 \text{ N/mm}^2$$

Stress at 'c'

3rd Quadrant (-, -)

$$\sigma_C = \frac{M'U}{I_{VV}} + \frac{M''V}{I_{UU}}$$

$$U = -x \cos \theta - y \sin \theta$$

$$= -15 \cos 20^\circ - 25 \sin 20^\circ$$

$$= -22.64 \text{ mm}$$

$$V = \frac{du}{d\theta} = -(x \sin \theta) - y \cos \theta$$

$$= 15 \times \sin 20^\circ - 25 \times \cos 20^\circ$$

$$= -18.36 \text{ mm}$$

$$\sigma_C = \frac{1.64 \times 10^5 \times -22.64}{11280} + \frac{4.51 \times 10^5 \times -18.36}{99875}$$

$$= -329.163 - 82.90$$

$$\sigma_C = -412.07 \text{ N/mm}^2$$

- 2) A beam of 'T' section of flange dimension is 100mm x 20mm, web dimension is 150mm x 10mm, is 2.5m length and is simply supported at its ends. It carries a load of 3.2 kN, inclined at 20° to the vertical and passing through the centroid of the section. Take $E = 200 \text{ GN/m}^2$. Calculate (i) the max. tensile stress and compressive stress. (ii) Deflection due to load (iii) position due to principle axis.

Given data,

The principle axis are

$$X-X = U-U, Y-Y = V-V.$$

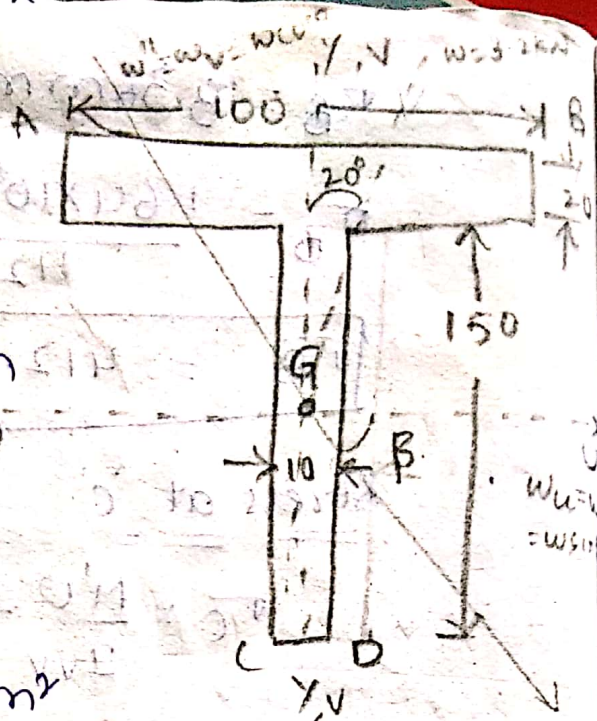
Then $l = 2.5 \text{ m} = 2500 \text{ mm}$

$$W = 3.2 \text{ kN.}$$

$$\theta = 20^\circ$$

$$E = 200 \text{ GN/m}^2$$

$$= 200 \times 10^3 \text{ N/mm}^2$$



for simply supported beam with point load

$$B.M = \frac{wl}{4} = \frac{3200 \times 2500}{4} = 20 \times 10^5 \text{ N}\cdot\text{mm}$$

$$\bar{x} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2} = \frac{(150 \times 10) \times \frac{100}{2} + (100 \times 20) \times 10}{(150 \times 10) + (100 \times 20)}$$

$$\therefore \bar{x} = 50 \text{ mm}$$

$$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2} = \frac{(150 \times 10) \times \frac{150}{2} + (100 \times 20) \times 150}{(150 \times 10) + (100 \times 20)}$$

$$\therefore \bar{y} = 123.57 \text{ mm from bottom.}$$

$$\bar{y} = 170 - 123.5 = 46.5 \text{ mm from top}$$

$$I_{xx} = \frac{bd^3}{12} + A x (\bar{y} - y_1)^2 + \frac{bd^3}{12} + A (\bar{y} - y_2)^2$$

$$= \frac{100 \times 20^3}{12} + (100 \times 20) \left(46.5 - \frac{20}{2}\right)^2 + \frac{10 \times 150^3}{12} + (10 \times 150) \left(46.5 - 20 + \frac{150}{2}\right)^2$$

$$= 27.31 \times 10^5 + 63.4 \times 10^5$$

$$I_{xx} = 90.7 \times 10^5 \text{ mm}^4$$

$$I_{yy} = \frac{db^3}{12} + A(\bar{x} - x_1)^2 + \frac{db^3}{12} + A(\bar{x} - x_2)^2$$

$$= \frac{20 \times 100^3}{12} + (20 \times 100)(50 - 50)^2 + \frac{150 \times 10^3}{12} + (150 \times 10)(50 - 50)^2$$

$$\therefore I_{yy} = 16.79 \times 10^5 \text{ mm}^4$$

components of (w)

$$w' = w \sin \theta = 3.2 \times 10^3 \times \sin 20^\circ = 1094.46 \text{ N}$$

$$w'' = w \cos \theta = 3.2 \times 10^3 \times \cos 20^\circ = 3007.01 \text{ N}$$

for simply supported beam with point load.

$$B.M = \frac{w\lambda}{4} = \frac{3.2 \times 2500}{4}$$

$$= 2000 \text{ kN}\cdot\text{mm}$$

In w consists of two components. i.e.,

w' and w''

$$M' = \frac{w'\lambda}{4} = \frac{1094.46 \times 2500}{4} = 684.03 \times 10^3 \text{ N}\cdot\text{mm}$$

$$M'' = \frac{w''\lambda}{4} = \frac{3007.01 \times 2500}{4} = 1.87 \times 10^6 \text{ N}\cdot\text{mm}$$

M' will cause max. compressive stress at

B & D. M'' will cause max. tensile stress

at C & D.

∴ Maximum tensile stress

$$\sigma = \frac{M'v}{I_{vv}} + \frac{M''v}{I_{vv}}$$

$$= \frac{684.03 \times 10^3}{I_{vv}}$$

A lies 2nd Quadrant $(-, +) = -50, +46.5$

$$v = x \cos \theta + y \sin \theta$$

$$= -50 \cos 20^\circ + 46.5 \times \sin 20^\circ$$

$$= -31.08 \text{ mm}$$



$$v = \frac{du}{d\theta} = -x \sin \theta + y \cos \theta$$

$$= -(-50 \sin 20^\circ + 46.5 \cos 20^\circ)$$

$$= 60.79 \text{ mm}$$

$$\sigma_A = \left(\frac{684.03 \times 10^3 \times (-31.08)}{16.79 \times 10^5} \right) + \left(\frac{1.87 \times 10^6 \times 60.79}{90.7 \times 10^5} \right)$$

$$= -12.66 + 12.53$$

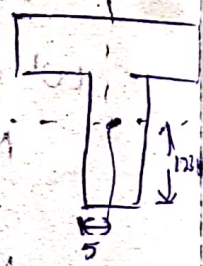
$$\therefore \sigma_A = -0.12 \text{ N/mm}^2$$

σ_C lies in 3rd Quadrant $(-, -) = (-5, -123.6)$

$$u = x \cos \theta + y \sin \theta$$

$$= 5 \cos 20^\circ + (-123.6 \times \sin 20^\circ)$$

$$= -46.97 \text{ mm}$$



$$v = -x \sin \theta + y \cos \theta$$

$$= -(-5 \sin 20^\circ) + (-123.6 \times \cos 20^\circ)$$

$$= -114.4 \text{ mm}$$

$$\sigma_C = \left(\frac{684.03 \times 10^3 \times (-46.97)}{16.79 \times 10^5} \right) + \left(\frac{1.87 \times 10^6 \times (-114.4)}{90.7 \times 10^5} \right)$$

$$= -19.13 + (-23.5)$$

$$\therefore \sigma_C = -42.7 \text{ N/mm}^2$$

'B' lies 1st Quadrant (+, +) (50, 46.5)

$$U = x \cos \theta + y \sin \theta$$
$$= 50 \times \cos 20^\circ + 46.5 \times \sin 20^\circ$$

$$= 62.88 \text{ mm}$$

$$V = -x \sin \theta + y \cos \theta$$

$$= -50 \sin 20^\circ + 46.5 \times \cos 20^\circ$$

$$= 26.59 \text{ mm}$$

$$\tau_B = \left(\frac{684.03 \times 10^3 \times (62.88)}{16.79 \times 10^5} \right) + \left(\frac{1.87 \times 10^6 \times 26.59}{90.7 \times 10^5} \right)$$

$$= 25.61 + 5.48$$

$$\therefore \tau_B = 31.092 \text{ N/mm}^2$$

'D' lies in 4th Quadrant (+, -) (+5, -123.6)

$$U = x \cos \theta + y \sin \theta$$
$$= 5 \cos 20^\circ + (-123.6 \sin 20^\circ)$$

$$= -37.5 \text{ mm}$$

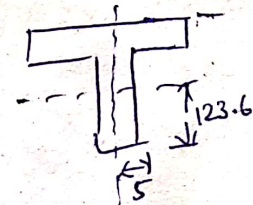
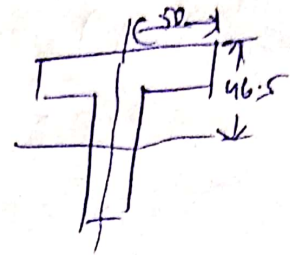
$$V = -x \sin \theta + y \cos \theta$$
$$= -5 \sin 20^\circ + (-123.6 \cos 20^\circ)$$

$$= -117.85 \text{ mm}$$

$$\tau_D = \frac{684.03 \times 10^3 \times (-37.5)}{16.79 \times 10^5} + \frac{1.87 \times 10^6 \times (-117.85)}{90.7 \times 10^5}$$

$$= -15.27 + (-24.29)$$

$$\therefore \tau_D = -39.56 \text{ N/mm}^2$$



(ii) Deflection of beam

$$\delta = \frac{Kw\ell^3}{E} \sqrt{\left(\frac{I_{VV}}{I_{UU}}\right)^2 + \left(\frac{I_{UU}}{I_{VV}}\right)^2}$$

'K' is constant for S.S Beam

$$= \frac{1}{48} \times \frac{3.2 \times 10^3 \times 2500^3}{200 \times 10^3} \sqrt{\left(\frac{I_{VV}}{16.79 \times 10^5}\right)^2 + \left(\frac{90.7 \times 10^5}{I_{VV}}\right)^2}$$

$$= 5.20 \times 10^6 \times 2.28 \times 10^{-7}$$

$$\therefore \boxed{\delta = 1.18 \text{ mm}}$$

(iii) Position of Neutral axis

$$\tan \beta = \frac{I_{UU}}{I_{VV}} \cdot \tan \theta$$

$$= \frac{90.7 \times 10^5}{16.79 \times 10^5} \times \tan 20^\circ$$

$$= \tan^{-1}(1.966)$$

$$\therefore \boxed{\beta = 63^\circ 2'}$$